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# **Gradient-Based Optimizer for Parameter Extraction in Photovoltaic Models**

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**ABSTRACT** Solar radiation is increasingly used as a clean energy source, and photovoltaic (PV) panels that contain solar cells (SCs) transform solar energy into electricity. The current-voltage characteristics for PV models is nonlinear. Due to a lack of data on the manufacturer's datasheet for PV models, there are several unknown parameters. It is necessary to accurately design the PV systems by defining the intrinsic parameters of the SCs. Various methods have been proposed to estimate the unknown parameters of PV cells. However, their results are often inaccurate. In this article, a gradient-based optimizer (GBO) was applied as an efficient and accurate methodology to estimate the parameters of SCs and PV modules. Three common SC models, namely, single-diode models (SDMs), double-diode models (DDMs), and three-diode models (TDMs) were used to demonstrate the capacity of the GBO to estimate the parameters of SCs. The proposed GBO algorithm for estimating the optimal values of the parameters for various SCs models are applied on the real data of a 55 mm diameter commercial R.T.C-France SC. Comparison between the GBO and other algorithms are performed for the same data set. The smallest value of the error between the experimental and the simulated data is achieved by the proposed GBO. Also, high closeness between the simulated P-V and I-V curves is achieved by the proposed GBO compared with the experimental.

**INDEX TERMS** Gradient-based optimizer, photovoltaic modules, diode models, renewable energy, solar energy.

## I. INTRODUCTION

Human life is stable due to energy, and improving life requires the development and progress of energy. As conventional sources of energy are depleted, they cause environmental exacerbation. Considering the above, the dependence on renewable energy sources is inevitable because it is clean, reduces environmental problems, exists in abundance, and has a variety of uses [1]–[3].

The main types of renewable energy sources are solar energy, wind energy, etc. Recently, a huge improvement in the performance of energy generated from these sources has been developed [4]–[6]. The use of clean and renewable energy sources is one of the most point in the research study [7]. One of the main renewable energy sources is the solar PV technology, that is used in several applications such as satellites [8], water desalination [9], cooling and heating [10]. So that the

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accurate modeling and simulation of solar cell is performed with several techniques such as adaptive control [11], [12] and numerical simulation [13]. The maintenance of SC panels is required [14].

SCs are constructed with semiconductor material of P-N junction that has a quasi-neutral region, space-charge region, and defect region. The losses in this region are due to the recombination and diffusion of the charge transporter. These losses must be considered in the development of the PV model. A photo-generated current is expressed in the ideal model of a PV cell. The value of the current generated from a real PV model veers about the experimental value due to losses in the semiconductor P-N junction. This leads to the establishment of the PV model in SDMs [15]. This model is simple and fast. Furthermore, the quasi-neutral region losses can be expressed into the SDM. Meanwhile, a DDM was applied to achieve higher accuracy. The DDM presents the losses expressed in the SDM and the space charge region losses. Meanwhile, a TDM was applied to achieve more

accuracy than the SDMs and DDMs. The losses expressed by the TDM were defect region losses and the ones described in the DDM [16].

To properly model the behavior of the PV modules, the diode representations possessed some parameters that could affect their output. They needed to be calibrated according to the information used in the design. There are five unknown parameters in SDMs, seven in DDMs, and nine in TDMs. These parameters are commonly estimated in two ways: by using metaheuristic optimization algorithms [17] and with iterative mathematical methods [18]. These parameters are estimated from multiple approaches, such as the iterative mathematical techniques that estimate five parameters by assuming the value of the ideality factor [18]. Also, the Lambert W-function method was applied to estimate these parameters from the datasheet of PV cells [19], [20]. The least squares method and the Gauss-Seidel method were used as an iterative approach in the parameter's extraction [21]–[24]. The complex and nonlinear optimization problem derived from the identification of internal parameters was solved with metaheuristic algorithms. This is possible due to the improvement of swarm intelligence and the development of computers [25].

Due to the nonlinearity behavior of photovoltaic models and increasing number of parameters required to be estimated, the metaheuristic algorithms are applied to achieve high accuracy for the extracted parameters. Several optimization techniques have been used for the extraction and estimation of PV parameters. The multiple learning backtracking search algorithm (MLBSA) was developed to estimate PV parameters with high accuracy and reliability in [26], in which the grey wolf optimizer (GWO) and the cuckoo search algorithm (CSA) were combined in a method called GWOCS to extract these parameters with the aim of achieving an appropriate balance between the exploration and exploitation in [27], and an opposition-based sine cosine approach with local search was used to identify the optimal parameters. This optimizer design was based on the exploratory and exploitative cores of the sine cosine algorithm (SCA) [28]. The parameters of PV cells were also identified using a logistic chaotic JAYA algorithm (LCJAYA) with high performance [29]. In the same context, the winner-leading competitive swarm optimizer with dynamic gaussian mutation [30] and covote optimization algorithm (COA) [31] are applied for extracting the photovoltaic parameters.

The seven unknown parameters in the DDM were extracted with different optimization techniques like the moth flame algorithm and the orthogonal nelder-mead moth flame optimization (NM-SOLMFO), which were applied to increase the accuracy and reliability of the optimization process in [32]. PV parameters were also identified by using the teaching learning-based and the improved teaching learning-based optimization algorithm (ITLBO) with high reliability and accuracy [33]. On the other hand, for TDM, some researchers assumed the value of the ideality-factor for the second and third diodes [34]. Then the parameters were estimated with methods like the interval branch and the bound global optimization algorithm [35]. Also, the simplified teaching learning-based optimization (STBLO) was applied to estimate the parameters in TDM [36]. Parameter extraction was prepared by an improved version of the whale optimization algorithm using the opposition-based learning (OBWOA) [37], the chaotic improved artificial bee colony (CIABC) [38], and Harris hawk optimization (HHO) [39].

In the related literature, several metaheuristic optimization algorithms have been applied to extract the PV parameters such as the traditional genetic algorithm (GA) and its improvements [40]-[42], the differential evolution with its generation [43]-[45], the artificial bee swarm algorithms [46], the improved ant lion algorithm [47], the salp swarm-inspired algorithm [48], [49], the bio-geography based optimization [50], the improved cuckoo search algorithm [51], the bird mating optimization [52], the hybrid bee pollinator flower pollination algorithm [53], the bacterial foraging algorithm [54] and the artificial immune system [55]. To estimate the parameter of SDMs, different approaches have been used like the boosted mutation-based Harris hawks optimizer [56], the improved electromagnetic-like algorithm [57], the grasshopper optimization algorithm [58], the improved whale optimization algorithm [59], and the shark smell optimizer [60].

## MOTIVATION AND CONTRIBUTIONS

Logically, No Free Lunch (NFL) theorem [61] has proved that there is no metaheuristic optimization technique for solving all optimization problems. According to this theorem, the superior performance of an optimizer on a class of problems cannot guarantee the similar performance on another class of problems. This theorem is the foundation of many work in the literature and allows researchers in this field to adapt the current techniques for new classes of problems. The purpose of this study is to propose an efficient search mechanism for estimating the unknown parameters of PV cells. In this study, a gradient-based optimizer (GBO) was applied to estimate the parameters of the three common SC models, namely, single-diode model (SDM), double-diode model (DDM), and three-diode model (TDM). The GBO algorithm shows a strong performance of parameter optimization, which has be proved in [62]. The GBO algorithm has various advantages, such as solution accuracy, balance, convergence speed, between analysis and exploitation and also shows a strong performance of parameter optimization, which has be proved in [62]. This is the foundation and motivation of this work as well, in which we apply GBO to solve this problem.

To summarize, the major contributions of this work are:

- The parameters of three models of PV cells were estimated with a new GBO to minimize the objective function.
- The validation of the GBO algorithm was performed by changing the PV models (SDM, DDM, and TDM).

- The parameters extracted from previous works and another two optimization algorithms were used for comparison with the proposed GBO algorithm over the same data set of R.T.C France solar cells.
- Statistical analysis was used to study the performance of the proposed GBO technique compared with other algorithms.
- The efficiency of the proposed GBO was verified by checking the value of absolute error of the current and power at the best root mean square.
- The P-V and I-V curves were simulated for the estimated parameters values to graphically verify the accuracy of the proposal.

The organization of this paper is as follows: Section II discusses the analysis of PV diode models, Section III explains the objective function, Section IV presents an overview for the GBO, the simulation and results are discussed in V, and the conclusion of this paper is illustrated in Section VI.

## **II. ANALYSIS OF PV MODELS**

Three PV models are analyzed in this section: SDMs, DDMs, and TDMs. They are electrical circuits that will be described in detail in the following subsections.

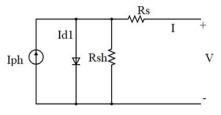


FIGURE 1. Equivalent circuit of the SDM.

#### A. ANALYSIS OF THE SINGLE DIODE MODEL

The equivalent circuit of the SDM is described in Figure 1. It contains only one diode that permits the shunting of the photogenerated current  $I_{ph}$ . In the SDM, the total current was computed by using the following equation:

$$I = I_{ph} - I_{d1} - I_{sh} \tag{1}$$

where, I is the total current,  $I_{ph}$  corresponds to the photogenerated current,  $I_{d1}$  is the diode current and  $I_{sh}$  is the shunt resistor current. Since the diode was constructed from semiconductor materials, some internal parameters can be manipulated to increase the quality of the output values. The Shockley diode equation helped to handle the intrinsic values of the diode. Considering this fact, Eq.(1) is rewritten as:

$$I = I_{ph} - I_{s1} \left( e^{\frac{q(V+IR_s)}{a_1 k T_c}} - 1 \right) - \left( \frac{V+IR_s}{R_{sh}} \right)$$
(2)

In Eq.(2), V is the total voltage,  $I_{s1}$  is the diode reverse saturation current,  $R_{sh}$  is the shunt resistance,  $R_s$  is the series resistance.  $a_1$  is the non-physical ideality factor,  $k = 1.3806503 \times 10^{-23} (J/K)$  is the Boltzmann's constant, the variable  $q = 1.60217646 \times 10^{-19} C$  is the charge of the electron, finally  $T_c$  is the temperature in Kelvin. The efficiency of the model is

provided by the outputs V and I and the unknown parameters of the SDM are  $(I_{ph}, I_{s1}, a_1, R_s, \text{ and } R_{sh})$ . As is expected, a proper configuration of such a parameter will directly affect the output.

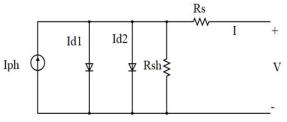


FIGURE 2. DDM equivalent circuit.

## B. ANALYSIS OF THE DOUBLE DIODE MODEL

Another interpretation of the PV modules is the DDM. Its equivalent circuit is described in Figure 2. The advantage of a DDM is that it considers the loss of recombination currents in the depletion region. Notice that the SDM does not include this information. The total current of the DDM is computed as follows:

$$I = I_{ph} - I_{d1} - I_{d2} - I_{sh}$$
(3)

By using the Shockley function the Eq.(3) can be rewritten as:

$$I = I_{ph} - I_{s1} \left( e^{\frac{q(V+IR_s)}{a_1 k T_c}} - 1 \right)$$
$$- I_{s2} \left( e^{\frac{q(V+IR_s)}{a_2 k T_c}} - 1 \right)$$
$$- \left( \frac{V+IR_s}{R_{sh}} \right)$$
(4)

In Eq.(4),  $I_{d2}$  is the saturation current for the second diode.  $a_2$  is the second diode ideality factor. As opposed to the SDM, the DDM has seven parameters that must be estimated and they are  $(I_{ph}, I_{s1}, a_1, R_s, R_{sh}, I_{s2}, and a_2)$ .

### C. ANALYSIS OF THE THREE DIODE MODEL

In the TDM, an extra diode is added to the DDM to consider and simulate the leakage current in the grain boundaries that are present in commercial CSs [63], [64]. The TDM equivalent circuit is described in Figure 3 and the total current is computed as:

$$I = I_{ph} - I_{d1} - I_{d2} - I_{d3} - I_{sh}$$
<sup>(5)</sup>

In Eq.(5) the Shockley function is replace for each diode. Then the result is the following equation:

$$I = I_{ph} - I_{s1} \left( e^{\frac{q(V+IR_s)}{a_1 K T_c}} - 1 \right) - I_{s2} \left( e^{\frac{q(V+IR_s)}{a_2 K T_c}} - 1 \right) - I_{s3} \left( e^{\frac{q(V+IR_s)}{a_3 K T_c}} - 1 \right) - \left( \frac{V+IR_s}{R_{sh}} \right)$$
(6)

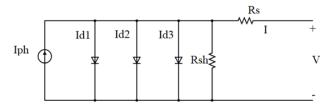


FIGURE 3. TDM equivalent circuit.

In Eq.(6),  $a_3$  is the third diode ideality factor, while  $I_{d3}$  is the third diode saturation current. Notice that the inclusion of a third diode also increases the number of parameter that must be properly estimated. The nine parameters are  $(I_{ph}, I_{s1}, a_1, R_s, R_{sh}, I_{s2}, a_2, I_{s3}, \text{ and } a_3)$ .

## III. THE OBJECTIVE FUNCTION FOR PHOTOVOLTAIC PARAMETER ESTIMATION

The optimization algorithms are used to extract the parameters of different models of PV cells. These techniques need an objective function that permits the evaluation of the candidate solutions. The optimization problems are defined in bounded spaces. These boundaries are defined in Table 1.

TABLE 1. The boundaries of extracted photovoltaic parameters [26].

Parameters	Lower bound	Upper bound
$I_{ph}(A)$	0	1
$I_{s1}, I_{s2}, I_{s3}(\mu A)$	0	1
$R_s(\Omega)$	0	0.5
$R_{sh}(\Omega)$	0	100
$a_1, a_2, a_3$	1	2

The root mean square error (RMSE) is the objective function and must be minimized by the optimizer technique. The X decision variables are extracted each time the optimizer is run. The mathematical formula to compute RMSE is defined as follows:

$$J(V, I, X) = I - I_{exp} \tag{7}$$

The vector of decision variables for the SDM is  $X = (I_{ph}, I_{s1}, a_1, R_s, R_{sh})$ . The vector of decision variables for the DDM is  $X = (I_{ph}, I_{s1}, a_1, R_s, R_{sh}, I_{s2}, a_2)$ . The vector of decision variables for the TDM is  $X = (I_{ph}, I_{s1}, a_1, R_s, R_{sh}, I_{s2}, a_2, I_{s3}, a_3)$ .

$$RMSE = \sqrt{1/N \sum_{i=1}^{N} (J(V, I, X))^2}$$
(8)

where  $I_{exp}$  is the experimental current and N is the reading data number.

#### **IV. GRADIENT-BASED OPTIMIZER**

A GBO [62] is based on the idea of the integration of population-based methods with a gradient technique to solve complex optimization problems. The GBO algorithm utilizes Newton's method to control the search agent's direction while exploring the problem space. The GBO algorithm has two basic components, including the gradient search rule and the locale escaping operator.

#### A. INITIALIZATION STAGE

Like most metaheuristic algorithms, the GBO starts the optimization process with an initial population generated independently from uniform random distribution. Each population agent is called a "vector", and the population has a number of N vector agents in a D-dimensional search space. The initialization process is then performed as follows:

$$X_n = X_{min} + rand(0, 1) \times (X_{max} - X_{min})$$
(9)

where  $X_{min}$ , and  $X_{max}$  are the bounds of decision variables X, and rand(0, 1) is a random number defined in the range [0, 1].

## **B. GRADIENT SEARCH RULE STAGE**

As mentioned previously, the GBO algorithm begins with a random set of initial solutions and updates each agent position depending on a gradient specified direction. To guarantee balance between exploration of significant search space regions and exploitation to reach near optimum and global points, a significant factor  $\rho_1$  is employed as follows:

$$\rho_1 = 2 \times \operatorname{rand} \times \alpha - \alpha \tag{10}$$

$$\alpha = \left| \beta \times \sin\left(\frac{3\pi}{2} + \sin\left(\beta \times \frac{3\pi}{2}\right)\right) \right| \tag{11}$$

$$\beta = \beta_{\min} + (\beta_{\max} - \beta_{\min}) \times \left(1 - \left(\frac{m}{M}\right)^3\right)^2 \quad (12)$$

where  $\beta_{\min}$  and  $\beta_{\max}$  are constant values 0.2 and 1.2, respectively, *m* represents the current iteration number, while *M* represents the total number of iterations. To balance the exploration and exploitation processes, the parameter  $\rho_1$  changes based on the sine function  $\alpha$ . This parameter value changes throughout the iterations. It starts with a large value through the first optimization iterations in order to improve population diversity. Then, the value decreases throughout iterations to accelerate population convergence. The parameter value increases throughout defined iterations within a range [550, 750], which in turn increases solution diversity and converges around the best obtained solution and the exploration of more solutions. Therefore, an algorithm is enabled to avoid local sub-regions. Thus, GSR can be determined as follows:

$$GSR = randn \times \rho_1 \times \frac{2\Delta x \times x_n}{(x_{\text{worst}} - x_{best} + \varepsilon)}$$
(13)

The concept of *GSR* provides the GBO algorithm with random behavior across iterations, therefore, strengthening exploration behavior and escaping from local optima. In Eq.(13), the factor  $\Delta x$  is defined and measures the difference between the best solution ( $x_{best}$ ) and a randomly selected solution  $x_{r1}^m$ . To ensure that  $\Delta x$  changes through iterations, the parameter  $\delta$  is computed by Eq.(16). Additionally, to improve exploration, a random number (randn) is added to this equation.

$$\Delta x = \operatorname{rand}(1:N) \times |\operatorname{step}| \tag{14}$$

$$\text{step} = \frac{\left(x_{\text{best}} - x_{r1}^{m}\right) + \delta}{2} \tag{15}$$

$$\delta = 2 \times \text{rand} \times \left( \left| \frac{x_{r1}^m + x_{r2}^m + x_{r3}^m + x_{r4}^m}{4} - x_n^m \right| \right) \quad (16)$$

The direction of movement (DM) is employed to converge around the area of solution  $x_n$ . This term uses the best vector and moves the current vector  $(x_n)$  in the direction of  $(x_{best} - x_n)$ . This process provide a convenient local search tendency with a significant affect on GBO convergence. The DM is computed with the following formula:

$$DM = rand \times \rho_2 \times (x_{best} - x_n) \tag{17}$$

where, rand is a uniform distributed number within range [0, 1], and  $\rho_2$  is a random parameter employed to modify step size of each vector agent. The  $\rho_2$  parameter considers of significant parameters of the GBO exploration process. The  $\rho_2$  parameter is computed as follows:

$$\rho_2 = 2 \times rand \times \alpha - \alpha. \tag{18}$$

Finally, depending on these terms GSR and DM, Eq.(19) and Eq.(20) are used to update the current vector  $(x_n^m)$  position.

$$X1_n^m = x_n^m - GSR + DM \tag{19}$$

where,  $X1_n^m$  is the new vector generated by updating  $x_n^m$ . According to Eq.(12) and Eq.(17), the  $X1_n^m$  can be reformulated as:

$$X1_n^m = x_n^m - randn \times \rho_1 \times \frac{2\Delta x \times x_n^m}{\left(yp_n^m - yq_n^m + \varepsilon\right)} + randn \times \rho_2 \times \left(x_{\text{best}} - x_n^m\right) \quad (20)$$

where  $yp_n^m$ ,  $yq_n^m$  are equal to  $y_n + \Delta x$ , and the  $y_n - \Delta x$ ,  $y_n$  vector is equal to the average of the two vectors: current solution  $x_n$  and  $z_{n+1}$  vector. This is calculated as follows:

$$z_{n+1} = x_n - randn \times \frac{2\Delta x \times x_n}{(x_{\text{worst}} - x_{\text{best}} + \varepsilon)}$$
(21)

while  $x_n$  represents the current solution vector, *randn* is a random solution vector of dimension n,  $x_{worst}$  and  $x_{best}$  represent worst and best solutions, and  $\Delta x$  is given by Eq.(14). Based on the previous formula, when replacing the best solution vector  $x_{best}$  with the current solution vector  $x_n^m$  we get  $X2_n^m$ the follows:

$$X2_n^m = x_{\text{best}} - randn \times \rho_1 \times \frac{2\Delta x \times x_n^m}{\left(yp_n^m - yq_n^m + \varepsilon\right)} + randn \times \rho_2 \times \left(x_{r1}^m - x_{r2}^m\right)$$
(22)

The GBO algorithm aims to enhance exploration and exploitation phases using Eq.(20) to improve the global search during the exploration phase, while Eq.(22) is used to improve the local search capability on exploitation phase. Finally, the new solution for the next iteration is generated as follows:

$$x_n^{m+1} = r_a \times \left( r_b \times X1_n^m + (1 - r_b) \times X2_n^m \right) + (1 - r_a) \times X3_n^m$$
(23)

where  $r_a$ , and  $r_b$  are random numbers determined in range [0, 1], and  $X3_n^m$  is defined as:

$$X3_n^m = X_n^{m+1} - \rho 1 \times (X2_n^m - X1_n^m)$$
(24)

#### C. LOCAL ESCAPING OPERATOR STAGE

The Local Escaping operator (LEO) is introduced to strengthen the performance of an optimization algorithm for solving complex problems. The LEO can effectively update the position of the solution. Hence, it assists an algorithm to get out of local optima points, and speed the convergence. The LEO uses targets to generate a new solution with superior performance  $(X_{LEO}^m)$  several solutions  $(X_{best}$  best solution, the solutions  $X_{r1}^m, X_{r2}^m$  randomly generated solutions). It effectively updates current solutions and the process is performed based on following scheme: If rand < pr

$$X_{LEO}^{m} = \begin{cases} X_{n}^{m+1} + f_{1} \left( u_{1} x_{\text{best}} - u_{2} x_{k}^{m} \right) \\ + f_{2} \rho_{1} \left( u_{3} \left( X 2_{n}^{m} - X 1_{n}^{m} \right) \right) \\ + u_{2} \left( x_{r1}^{m} - x_{r2}^{m} \right) / 2, & \text{if rand } < 0.5 \\ X_{n}^{m+1} + f_{1} \left( u_{1} x_{\text{best}} - u_{2} x_{k}^{m} \right) \\ + f_{2} \rho_{1} \left( u_{3} \left( X 2_{n}^{m} - X 1_{n}^{m} \right) \right) \\ + u_{2} \left( x_{r1}^{m} - x_{r2}^{m} \right) / 2, & \text{otherwise} \end{cases}$$
(25)

End

where pr is a probability value, pr = 0.5, the values  $f_1$ , and  $f_2$  are uniform distributed random numbers  $\in [-1, 1]$ , and  $u_1, u_2, u_3$  are random values generated as following:

$$u_1 = \begin{cases} 2 \times \text{rand} & \text{if } \mu_1 < 0.5\\ 1 & \text{otherwise} \end{cases}$$
(26)

$$u_2 = \begin{cases} \text{rand} & \text{if } \mu_1 < 0.5\\ 1 & \text{otherwise} \end{cases}$$
(27)

$$u_3 = \begin{cases} \text{rand} & \text{if } \mu_1 < 0.5\\ 1 & \text{otherwise} \end{cases}$$
(28)

where *rand* represents a random number  $\in [0, 1]$ , and  $\mu_1$  is a number in range [0, 1]. The previous equations for  $u_1, u_2, u_3$ , can be simply explained as follows:

$$u_1 = L_1 \times 2 \times rand + (1 - L_1)$$
(29)

$$u_2 = L_1 \times rand + (1 - L_1) \tag{30}$$

$$u_3 = L_1 \times rand + (1 - L_1) \tag{31}$$

where  $L_1$  is a binary parameter takes value 0, 1, if parameter  $\mu_1 < 0.5$ , then value of  $L_1 = 1$ , otherwise  $L_1 = 0$ . The solution  $x_k^m$  is generated as follows:

$$x_k^m = \begin{cases} x_{\text{rand}} & \text{if } \mu_2 < 0.5\\ x_p^m & \text{otherwise} \end{cases}$$
(32)

*x<sub>rand</sub>* is a random generated solution according to following formula:

$$x_{\text{rand}} = X_{\min} + \operatorname{rand}(0, 1) \times (X_{\max} - X_{\min})$$
(33)

Algorithm 1 The Pseudo Code of the Gradient-Based Optimizer	
Step 1. Initialization	
Assign values for parameters $pr$ , $\varepsilon$ , $M$	
Generate an initial population $X_0 = [x_{0,1}, x_{0,2}, \dots, x_{o,D}]$	
Evaluate the objective function value $f(X_0) =, n = 1,, N$	
Specify the best and worst solutions $x_{best}^m$ and $x_{worst}^m$	
Step 2. Main loop	
while $m < M$ do	
for $n = 1$ to N do	
for $n = 1$ to D do	
Select randomly $r1 \neq r2 \neq r3 \neq r4 \neq n$ in the range of $[1, N]$	
Calculate the position $x_{n,i}^{m+1}$ using Eq. (23)	
end for	
if rand < pr then	Local escaping operator
Calculate the position $x_{LEO}^m$ using Eq. (25)	
$x_n^{m+1} = x_{LEO}^m$	
end if	
Update the positions $x_{best}^m$ and $x_{worst}^m$	
end for	
m = m + 1	
end while	
Step 2. Return $x_{best}^m$	

 $x_p^m$  is a random selected solution from population and  $\mu_2$  is a random number  $\in [0, 1]$ .

Algorithm 1 describes the details pseudo-code of GBO algorithm.

# **V. ANALYSIS OF RESULTS**

For fair benchmarking comparison, the GBO algorithm and the competitive algorithms have been tested with 30 independent runs and pr is set to 0.5 (default value). As demonstrated in [65], setting algorithm parameters to their default values is a fair and appropriate practice.

This section presents the analysis of the parameters extracted by the proposed GBO algorithm for various PV models. The objective function is optimized by the GBO. Other interesting approaches are also used for this problem, for example, the moth flame optimization (MFO) algorithm and cuckoo search algorithm (CSA). The performance of GBO was validated by the comparison of its results with other algorithms from previous work and with the CSA and MFO. In the following section, the primary discussion drawn from this study will be presented as well as the details of the extracted parameters, and the best RMSE by algorithms is performed.

The reported results are divided into three terms: the first data is the extracted parameters of each optimization algorithm at the best objective function (root mean square error); the second is the value of the simulated current and power at the parameters that achieve the best objective function extracted from the proposed GBO; then, based on the simulated current and power and the experimental power and current data, the absolute error for current data and the absolute error for power data are calculated; and the final

data is the statistical analysis (minimum RMSE, mean of RMSE, maximum RMSE and standard deviation of RMSE) of the results extracted from all algorithms. These results are calculated for the SDM, DDM, and TDM.

## A. RESULTS USING THE SINGLE-DIODE MODEL

The comparison of the results for SDM is presented in Table 2. This table includes the best RMSE and the parameters extracted from each algorithm. Based on the output data in Table 2, the RMSE of value 7.7301E-04 is achieved by COA and the best value of RMSE (9.8602E-4) was achieved by the GBO algorithm, together with ISCA, NMSOLMFO, ITLBO and MLBSA. While the second best RMSE (9.8607E-4) was achieved by GWOCS, followed by MFO, CSA, JAYA, LCJAYA and GWO respectively. The accuracy of the parameter values was measured by the RMSE. The absolute error (AE) for each value of power and current between the simulated and measured data was performed to evaluate the quality of the results shown in Table 3. The maximum value of AE for power was 1.462574E-03 and this current was less than 2.5085074E-03. The values of RMSE and AE for current and power confirm the quality and accuracy of the extracted parameters. The P-V and I-V curves for the SDM were based on the estimated data from the GBO at the best RMSE which is explained in Figure 4. In this figure, the proposed GBO was validated by comparing the simulation result with the experimental data of the R.T.C France solar cell. From this figure, it was observed that the simulation data output from the proposed GBO for SDM aligned with the measured data. So, the performance of the SDM based on GBO algorithm was more efficient.

Algorithm	$I_{ph}(A)$	$I_{s1}(\mu A)$	$a_1$	$R_s(\Omega)$	$R_{sh}(\Omega)$	RMSE
GBO	0.76077553	0.32302	1.481183596	0.036377092	53.71852549	9.8602E-04
MFO	0.760796012	0.3086	1.476593356	0.036557977	52.50655869	0.000989856
CSA	0.760892912	3.18E-07	1.479628661	0.036455939	52.44667219	0.000991184
MLBSA [26]	0.7608	0.323	1.4812	0.0364	53.7185	9.8600
MLBSA [26]	0.7608	0.323	1.4812	0.0364	53.7185	9.8602E-04
GWOCS [27]	0.760773	0.32192	1.4808	0.03639	53.632	9.8607E-04
GWO [27]	0.769969	0.91215	1.596658	0.02928	18.103	7.5011E-03
ISCA [28]	0.76077562	0.323017	1.4811822	0.03637716	53.71821748	9.8602E-04
LCJAYA [29]	0.7608	0.323	1.4819	0.0364	53.7185	0.004762841937654
JAYA [29]	0.7608	0.3281	1.4828	0.0364	54.9298	0.00255675552142
COA [31]	0.760788	0.31069	1.47727	0.03655	52.8898	7.7301E-04
ITLBO [33]	0.7608	0.323	1.4812	0.0364	53.7185	9.8602E-04

#### TABLE 2. The parameters estimated for single diode model at the best root mean square error (RMSE).

#### TABLE 3. Absolute error (AE) of single diode model at the best root mean square error using gradient-based optimizer.

Items	Real data				power simulated	d data
nums	V(V)	$I_{exp}(A)$	$I_{sim}(A)$	$AE_I(A)$	$P_{sim}(w)$	$AE_P(w)$
1	-0.2057	0.764	0.764087704	8.77037E-05	-0.157172841	1.80407E-05
2	-0.1291	0.762	0.762663086	0.000663086	-0.098459804	8.56044E-05
3	-0.0588	0.7605	0.761355307	0.000855307	-0.044767692	5.02921E-05
4	0.0057	0.7605	0.760153991	0.000346009	0.004332878	1.97225E-06
5	0.0646	0.76	0.759055209	0.000944791	0.049034966	6.10335E-05
6	0.1185	0.759	0.758042345	0.000957655	0.089828018	0.000113482
7	0.1678	0.757	0.757091654	9.16539E-05	0.12703998	1.53795E-05
8	0.2132	0.757	0.756141365	0.000858635	0.161209339	0.000183061
9	0.2545	0.7555	0.755086873	0.000413127	0.192169609	0.000105141
10	0.2924	0.754	0.753663878	0.000336122	0.220371318	9.8282E-05
11	0.3269	0.7505	0.751390967	0.000890967	0.245629707	0.000291257
12	0.3585	0.7465	0.747353851	0.000853851	0.267926356	0.000306106
13	0.3873	0.7385	0.740117222	0.001617222	0.2866474	0.00062635
14	0.4137	0.728	0.727382225	0.000617775	0.300918027	0.000255573
15	0.4373	0.7065	0.706972651	0.000472651	0.30915914	0.00020669
16	0.459	0.6755	0.675280151	0.000219849	0.30995359	0.00010091
17	0.4784	0.632	0.630758272	0.001241728	0.301754758	0.000594042
18	0.496	0.573	0.571928358	0.001071642	0.283676466	0.000531534
19	0.5119	0.499	0.499607019	0.000607019	0.255748833	0.000310733
20	0.5265	0.413	0.413648792	0.000648792	0.217786089	0.000341589
21	0.5398	0.3165	0.31751011	0.00101011	0.171391957	0.000545257
22	0.5521	0.212	0.21215494	0.00015494	0.117130742	8.55421E-05
23	0.5633	0.1035	0.102251312	0.001248688	0.057598164	0.000703386
24	0.5736	-0.01	-0.008717541	0.001282459	-0.005000382	0.000735618
25	0.5833	-0.123	-0.125507413	0.002507413	-0.073208474	0.001462574
26	0.59	-0.21	-0.208472327	0.001527673	-0.122998673	0.000901327

## **B. RESULTS USING THE DOUBLE-DIODE MODEL**

A comparative study of the results based on the DDM was introduced in Table 4. It includes the parameters extracted from each algorithm at the best RMSE. The results in Table 4, the best RMSE value (9.8237E-4) was achieved by ISCA algorithm, and the second best RMSE (9.8249E-4) was achieved by ITLBO together nearly with MLBSA. The third best RMSE (9.8258E-4) was computed from the GBO algorithm, followed by GWOCS, MFO, CSA, GWO, JAYA and LCJAYA, respectively. As for the SDM, the accuracy of the parameters was evaluated from the RMSE. The absolute error (AE) was also used for the current and power values in a comparison between the measured data presented in Table 5. The value of the AE for power was less than 1.48807E-03 and the maximum value of AE for current and power confirmed the

quality and accuracy of the estimated parameters. The P-V and I-V curves for the DDM was based on the estimated data from GBO at the best RMSE, as explained in Figure 5. In this figure, the proposed GBO was validated by comparing the simulation result with the experimental data of R.T.C France solar cell. From this figure, it was observed that the simulation data output from the proposed GBO for double diode model aligned with the measured data. Thus, the performance of the DDM based on the GBO algorithm was more efficient.

## C. RESULTS USING THE THREE-DIODE MODEL

A comparative study of the results based on the TDM is introduced in Table 6. The table shows the best RMSE and the parameters extracted from each algorithm. From Table 6, the optimal RMSE value (9.8249E-4) was achieved from the OBWOA algorithm, and the second best RMSE (9.82503E-4)

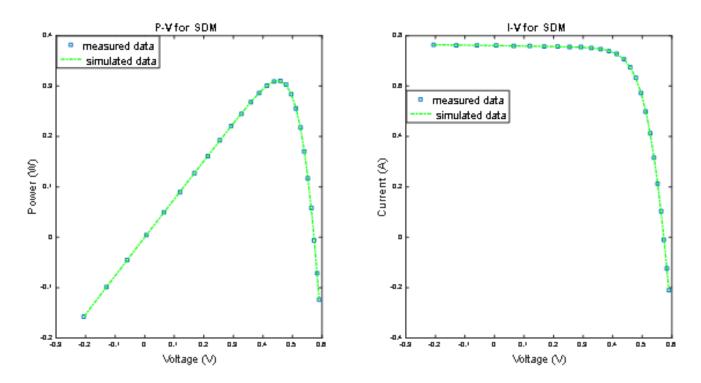


FIGURE 4. P-V and I-V curves for single diode model based on parameters extracted from gradient based optimizer.

TABLE 4. The parameters estimated of a double diode model at the best RMSE
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Algorithm	$I_{ph}(A)$	$I_{s1}(\mu A)$	$a_1$	$R_s(\Omega)$	$R_{sh}(\Omega)$	$I_{s2}(\mu A)$	$a_2$	RMSE
GBO	0.760780326	0.85705	1.999776183	0.036793056	55.7767015	0.2138	1.446432096	0.00098258
MFO	0.760843583	0.15736	1.421450251	0.037341537	52.92204541	0.7311	1.884225056	0.001007522
CSA	0.761759863	0.17618	1.429484164	0.037192705	46.45538652	0.96678	1.984563559	0.001123499
MLBSA [26]	0.7608	0.2273	1.4515	0.0367	55.4612	0.7384	2	0.00098249
GWOCS [27]	0.76076	0.53772	2	0.03666	54.7331	0.24855	1.4588	0.00098334
GWO [27]	0.761668	0.40302	1.646	0.03265	72.52775	0.45338	1.5527	0.0022124
ISCA [28]	0.760781079	0.7493463	2	0.036740424	55.48542959	0.22597411	1.4510169	0.00098237
LCJAYA [29]	0.7608	0.22596	1.4518	0.0367	55.4815	0.7464	2	0.00503457049
JAYA [29]	0.7607	0.0060763	1.8436	0.0364	52.6575	0.31507	1.4788	0.00227494479
COA [31]	0.76081	0.08656	1.37278	0.03803	52.3562	0.21597	2	7.3265E-04
ITLBO [33]	0.7608	0.226	1.451	0.0367	55.4854	0.7493	2	0.00098248

was achieved from the GBO, followed by STLBO, CIABS, MFO and CSA, respectively. Regarding the accuracy of the parameters obtained, RMSE was used as a proper metric. The AE was also used to verify the similarity between the simulated data and the measured data of the same data set used in Table 7. The value of AE for power was less than 1.485E-03 and the maximum value of AE for the current was 2.54586E-03. The values of RMSE and AE for the current and power confirmed the quality and accuracy of the extracted parameters. The P-V and I-V curves for the TDM were based on the estimated data from GBO at the best RMSE, as explained in Figure 6. In this figure, the proposed GBO was validated by comparing the simulation result with the experimental data of the R.T.C France solar cell. From this figure, it was observed that the simulation data output from the proposed GBO for three diode model aligned with the measured data. Thus, the performance of the TDM based on the GBO algorithm was more efficient.

## D. STATISTICAL ANALYSIS

The accuracy and performance of all used algorithms are evaluated in this subsection. This evaluation was based on the values of RMSE for 30 independent runs of each algorithm. Table 8 shows the statistical analysis for each algorithm in all three PV models. The accuracy of an algorithm is indicated by the minimum value of RMSE, whereas the mean accuracy is reflected by the average RMSE, and the reliability of the system is reflected by the standard deviation (SD). Based on the results presented in Table 8, it was observed that the proposed GBO, MLBSA, LCJAYA, and ITLBO achieved the best accuracy and reliability in the SDM. The proposed GBO achieved the second-best accuracy in the DDM. Meanwhile,

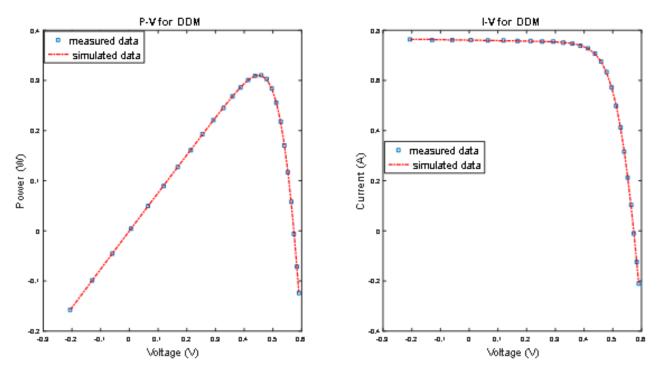


FIGURE 5. P-V and I-V curves for double diode model based on parameters extracted from gradient-based optimizer.

TABLE 5.	Absolute error (AE) of double diode model at the best RMSE
using gra	dient-based optimizer.

Current simulated data		Power simulated data		
$I_{sim}(A)$	$AE_I(A)$	$P_{sim}(w)$	$AE_P(w)$	
0.763965313	3.46867E-05	-0.157147665	7.13506E-06	
0.76259319	0.00059319	-0.098450781	7.65808E-05	
0.761333364	0.000833364	-0.044766402	4.90018E-05	
0.760175401	0.000324599	0.004333	1.85021E-06	
0.759114502	0.000885498	0.049038797	5.72032E-05	
0.758132509	0.000867491	0.089838702	0.000102798	
0.75720262	0.00020262	0.1270586	3.39996E-05	
0.756258569	0.000741431	0.161234327	0.000158073	
0.755190525	0.000309475	0.192195989	7.87613E-05	
0.753730606	0.000269394	0.220390829	7.87709E-05	
0.751399367	0.000899367	0.245632453	0.000294003	
0.74729178	0.00079178	0.267904103	0.000283853	
0.739991809	0.001491809	0.286598828	0.000577778	
0.727222708	0.000777292	0.300852034	0.000321566	
0.706827301	0.000327301	0.309095579	0.000143129	
0.675195557	0.000304443	0.309914761	0.000139739	
0.630757708	0.001242292	0.301754487	0.000594313	
0.572003297	0.000996703	0.283713635	0.000494365	
0.499722096	0.000722096	0.255807741	0.000369641	
0.413749921	0.000749921	0.217839333	0.000394833	
0.31755683	0.00105683	0.171417177	0.000570477	
0.21212393	0.00012393	0.117113622	6.84219E-05	
0.102154801	0.001345199	0.0575438	0.00075775	
-0.008800848	0.001199152	-0.005048167	0.000687833	
-0.125551133	0.002551133	-0.073233976	0.001488076	
-0.208363083	0.001636917	-0.122934219	0.000965781	

the proposed GBO achieved the best accuracy and reliability in TDM.

## E. ANALYSIS OF CONVERGENCE AND ROBUSTNESS

To graphically illustrate the robustness of the GBO against other algorithms, the convergence curves and robustness analysis are presented in this section. Figures 7, 8 and 9 explain the robustness and convergence curves of GBO, MFO, and CSA for the SDM, DDM, and TDM, respectively. The reliable robustness and faster convergence from these figures were from the GBO algorithm. The GBO reached a stable point for all PV models, and this behavior suggests that the GBO has good convergence capabilities. Figures 7, 8 and 9 show the convergence curves of all optimization algorithms for determining the parameters of PV modules for single, double, and three diode models, respectively. It was shown that the proposed algorithm (GBO) was the best one because it reached the minimum (best) value of the RMSE while the remaining algorithms did not reach to the best value of RMSE as the GBO.

In summary, the experimental results provided the following:

- The promising results obtained using the SDM, DDM, and TDM strongly prove that the GBO algorithm performs well in terms of RMSE, AE, and convergence and led to the optimal solutions shown in Sections V-D and V-E.
- The GBO algorithm showed superiority compared to the other algorithms in terms of RMSE, as shown in Table 2, 4 and 6.
- The GBO algorithm outperforms the other algorithms in term of AE, as shown in Tables 3, 5 and 7.
- The convergence curves and robustness behavior presented in Figures 7, 8 and 9 revealed that the GBO algorithm has better exploration and exploitation abilities than the other algorithms.

Overall, the solution extracted from the GBO converged to the global optima solution, and there were terms to determine

Algorithm	GBO	MFO	CSA	STLBO [36]	OBWOA [37]	CIABS [38]
$I_{ph}(A)$	0.760776979	7.61E-01	0.760358849	0.7608	0.76077	0.7607
$I_{s1}(\mu A)$	0.78129	0.42389	0	0.2349	0.2353	0.2
$a_1$	1.999994539	1.65E+00	1.826602665	1.44541	1.4543	1.4414
$R_s(\Omega)$	0.036758301	0.037131537	0.036699785	0.0367	0.03668	0.03687
$R_{sh}(\Omega)$	55.62330625	53.31146589	58.93317382	55.2641	55.4448	55.8344
$I_{s2}(\mu)$	0.221556	0.08147	0.15567	0.2297	0.2213	0.5
$a_2$	1.449384849	1.390944125	2	2	2	1.9
$I_{s3}(\mu A)$	0.00721	0.01843	0.2912	0.4443	0.4573	0.21
$a_3$	1.975652602	1.466698272	1.471740942	2	2	2
RMSE	0.000982503	0.000997027	0.001037665	9.8253E-04	9.8249E-04	9.8466E-04

# TABLE 6. The parameters estimated for three diode model at the best RMSE.

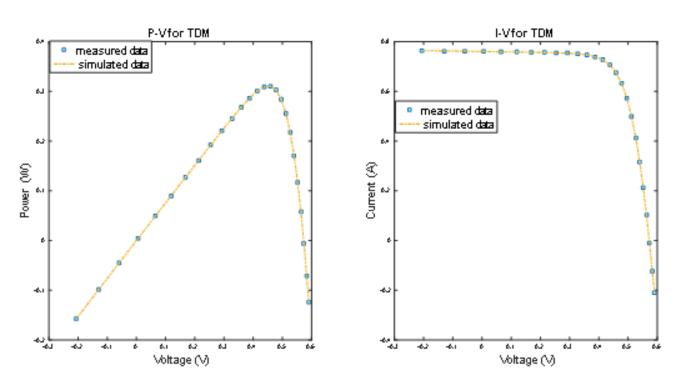


FIGURE 6. P-V and I-V curves for three diode model based on parameters extracted from gradient-based optimizer.

the quality of the solution. These terms were the mean and standard deviation for the 30 independent runs of the algorithms. Based on these runs, the robustness of the optimum solution was drawing like in Figures 7, 8, 9. From these figures, it was observed that the optimum solution for each run in nearly to each other over than other algorithms. The value of the standard deviation for the SDM was 1.7E-10. This value was indicated by all solutions of all runs and was approximately equal. Thus, the optimum solution of the GBO algorithm was converging to the global optima.

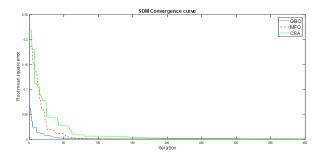
## F. DISCUSSION

The purpose of this study is to propose an efficient search mechanism for optimizing the unknown's parameters of PV models. The experimental analysis and comparative study performed in earlier section suggest that proved the efficacy of GBO compared to the counterparts. The GBO algorithm presents certain advantages:

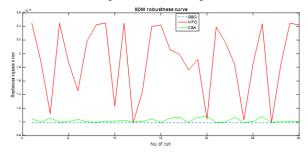
- The GBO is well able to perform an efficient search on the optimization landscapes that maintain varying difficulties and complexities. The GBO generates optimization solution with better fitness values than original and various other competitor methods. See Tables 2, 4, and 6.
- Also, in terms of Absolute error (AE), the GBO obtained the best AE values for each value of power and current between the simulated and measured data is performed to evaluate the results quality as shown in Tables 3, 5, and 7.
- Statistically, the optimization solutions generated by the GBO are significantly different than the ones generated by the various other optimization methods.
- The design of GBO is simple. Therefore, any opportunity to further enhance the algorithm is easy to implement.

 TABLE 7. (AE) Absolute error of three diode model at the best root mean square error using gradient-based optimizer.

Current simulat	ed data	Power simulated data		
$I_{sim}(A)$	$AE_I(A)$	$P_{sim}(w)$	$AE_P(w)$	
0.763971166	2.88345E-05	-0.157148869	5.93125E-06	
0.762595264	0.000595264	-0.098451049	7.68486E-05	
0.76133199	0.00083199	-0.044766321	4.8921E-05	
0.760170916	0.000329084	0.004332974	1.87578E-06	
0.759107317	0.000892683	0.049038333	5.76673E-05	
0.758123169	0.000876831	0.089837596	0.000103904	
0.757191932	0.000191932	0.127056806	3.22062E-05	
0.75624773	0.00075227	0.161232016	0.000160384	
0.755181181	0.000318819	0.192193611	8.11394E-05	
0.753724729	0.000275271	0.220389111	8.04892E-05	
0.751398776	0.000898776	0.24563226	0.00029381	
0.747297507	0.000797507	0.267906156	0.000285906	
0.740003203	0.001503203	0.28660324	0.00058219	
0.727237139	0.000762861	0.300858004	0.000315596	
0.706840388	0.000340388	0.309101302	0.000148852	
0.675202941	0.000297059	0.30991815	0.00013635	
0.630757017	0.001242983	0.301754157	0.000594643	
0.571994999	0.001005001	0.28370952	0.00049848	
0.499709205	0.000709205	0.255801142	0.000363042	
0.413737299	0.000737299	0.217832688	0.000388188	
0.317548455	0.001048455	0.171412656	0.000565956	
0.212122489	0.000122489	0.117112826	6.76263E-05	
0.102160033	0.001339967	0.057546746	0.000754804	
-0.008794868	0.001205132	-0.005044736	0.000691264	
-0.125545865	0.002545865	-0.073230903	0.001485003	
-0.20836846	0.00163154	-0.122937391	0.000962609	



(a) The convergence curve for single diode model

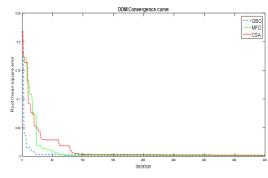


(b) The robustness curve for the single diode model

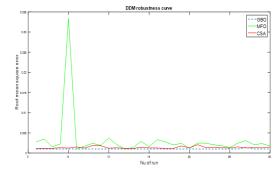
**FIGURE 7.** The convergence and robustness curves for single diode model.

Besides benefits, the GBO also poses some limitations as discussed below:

 In this GBO, ρ<sub>1</sub> is introduced as the most significant parameter in the GBO to balance the exploration and

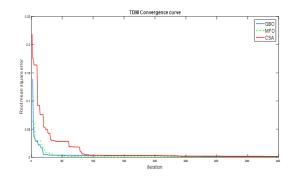


(a) The convergence curve for the double diode model.

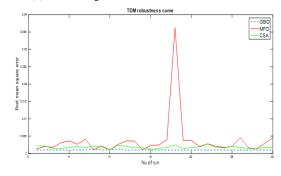


(b) The robustness curve for the double diode model.

FIGURE 8. The convergence and robustness curves for the double diode model.



(a) The convergence curve for the three diode model.



(b) The robustness curve for the three diode model.

**FIGURE 9.** The convergence and robustness curves for the three diode model.

exploitation searching processes. Thus modification in this parameter deems tricky when employed on optimization problems with difficult problem landscapes

Model	Algorithm		RM	SE	
Widder	Aigorium	Min	Max	Average	SD
	GBO	9.8602E-04	9.8602E-04	9.8602E-04	1.753E-10
	MFO	0.000989856	0.002448049	0.001912964	5.22926E-04
	CSA	9.91184E-04	1.081737E-03	1.021315E-03	2.94913E-05
	GWOCS [27]	9.8607E-04	9.9095E-04	9.8874E-04	2.4696E-06
SDM	GWO [27]	7.5011E-03	3.8160E-02	2.5617-02	1.6071E-02
SDM	ISCA [28]	7.34231E-04	7.45921E-04	7.23043E-04	1.30287E-06
	LCJAYA [29]	9.86E-04	9.86E-04	9.86E-04	5.70E-16
	JAYA [29]	9.8946E-04	1.4783E-03	1.1617E-03	1.8796E-04
	ITLBO [33]	9.8602E-04	9.8602E-04	9.8602E-04	2.19E-17
	MLBSA [26]	9.8602-04	9.8602E-04	9.8602 E-04	9.15E-12
	GBO	9.825797E-04	1.00054E-03	1.38203E-03	7.231E-05
	MFO	1.00752E-03	3.34096E-02	3.21918E-03	5.74432E-03
	CSA	1.12349E-03	2.07298E-03	1.35984E-03	2.366E-04
	GWOCS [27]	9.8334E-04	1.0017E-03	9.9411E-04	9.5937E-06
DDM	GWO [27]	2.2124E-03	3.7996E-02	1.6222E-02	1.9113E-02
	ISCA [28]	9.8342E-04	9.86863E-04	9.83800E-04	1.65397E-06
	LCJAYA [29]	9.83E-04	9.86E-04	9.83E-04	1.31E-06
	JAYA [29]	1.31E-06	1.4793E-03	1.1767E-03	1.9356E-04
	ITLBO [33]	9.8248E-04	9.8812E-04	9.8497E-04	1.54E-06
	MLBSA [26]	9.8249E-04	9.8249E-04	9.8518E-04	1.35E-06
	GBO	9.82503E-04	1.3636E-03	9.84283E-04	9.391E-05
TDM	MFO	9.97027E-04	3.62978E-02	3.7394E-03	6.2405E-03
	CSA	1.03766E-03	2.764015E-03	1.788847E-03	3.74083E-04

#### TABLE 8. Statistical analysis of root mean square error for three photovoltaic models.

- The parameter  $\alpha$  changes with the iteration number. It has a large value at the early iterations to enhance the population diversity and then its value decreases as the iteration number increases to accelerate the convergence, thus this dependent on the problem type.
- Because GBO is an optimization technique based on randomization, its selected values may vary every time it is run. Therefore, there is no guarantee that the values subset selected in one run can be found in another run, which may bring confusion for the end user.

## **VI. CONCLUSION AND FUTURE WORK**

This paper presented a new application of the GBO to estimate the parameters of three PV models. The three models were SDM, DDM, and TDM. The main idea of this work was to efficiently design the three PV models from the proper estimation of their parameters. The single diode mathematical model was formulated as a nonlinear equation between the current and voltage, including five unknown parameters due to the manufacture datasheet's shortage of data. Also, the DDM and TDM operated like the SDM, except the number of unknown parameters in the DDM is seven and in TDM is nine. The objective function of the extracted parameters in the three PV model was minimizing the root mean square error between the simulated current and the experimental current of the R.T.C France solar cell. The proposed GBO is a recent optimization technique employed to minimize the objective function of the parameter extraction of PV cells by using the SDM, DDM, and TDM. The GBO algorithm has various advantages, such as solution accuracy, balance, and convergence speed between analysis and exploitation. The results achieved by the GBO were more accurate than those achieved by most of the ten competitor algorithms. The GBO is, thus, a good candidate for solving the optimization problems of solar cell systems. In future work, the GBO can be applied to identify the PV parameters multidimensional diode and models, and also for calculating the current voltage characteristics of multi-diode diodes and models.

#### **CONFLICT OF INTEREST**

The authors declare that there is no conflict of interest. Non-financial competing interests.

#### **CREDIT AUTHOR STATEMENT**

Alaa A. K. Ismaeel: Methodology, Formal analysis, Writing - review & editing. Essam H. Houssein: Supervision, Methodology, Conceptualization, Formal analysis, Writing review & editing. Mokhtar Said: Software, Formal analysis, Resources, Writing - original draft. Diego Oliva: Conceptualization, Methodology, Formal analysis, Writing - review & editing. All authors read and approved the final paper.

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